

Das vollständige System trichotomischer Triaden

1. Im folgenden stellen wir das vollständige System der $3^3 = 27$ ternären semiotischen Relationen in Form von trajektischen Abbildungen der Form

$$T = (1, 2, 3) | (1, 2, 3) \text{ mit } | = R((1, 2, 3), (1, 2, 3))$$

dar (vgl. Toth 2025) und analysieren semiotische Relationen als Kompositionen dyadischer Teilrelationen (vgl. Walther 1979, S. 79)

$$(3.x, 2.y, 1.z) = (3.x \rightarrow 2.y) \circ (2.y \rightarrow 1.z)$$

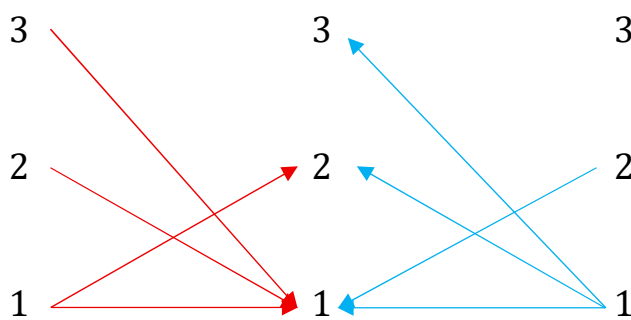
$$(z.1, y.2, x.3) = (z.1 \rightarrow y.2) \circ (y.2 \rightarrow x.3).$$

2. Trichotomische Triaden

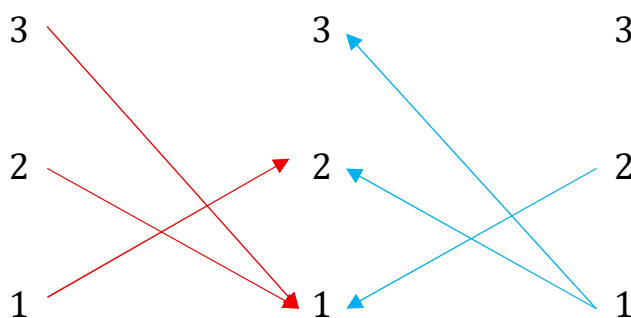
Zu Trichotomischen Triaden vgl. Bense (1975, S. 100 ff.), Walther (1981, 1982) u. Bense (1992, S. 76).

2.1. Erste TT

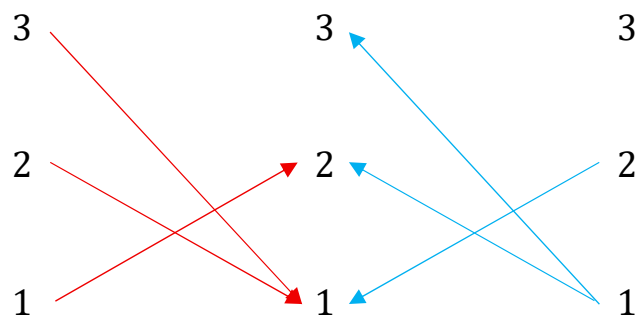
$$1. DS = [(3.1, 2.1, 1.1) \times (1.1, 1.2, 1.3)]$$



$$2. DS = [(3.1, 2.1, 1.2) \times (2.1, 1.2, 1.3)]$$

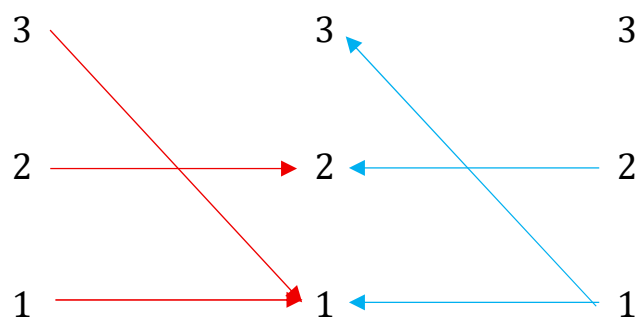


$$3. DS = [(3.1, 2.1, 1.3) \times (3.1, 1.2, 1.3)]$$

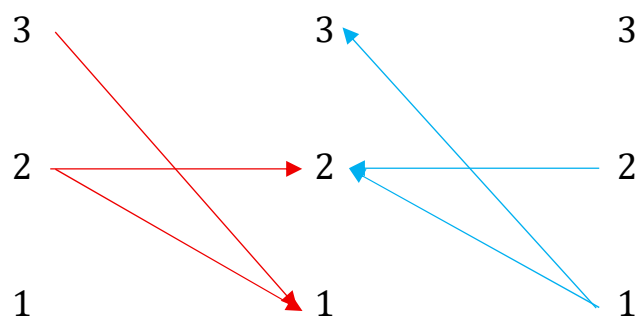


2.2. Zweite TT

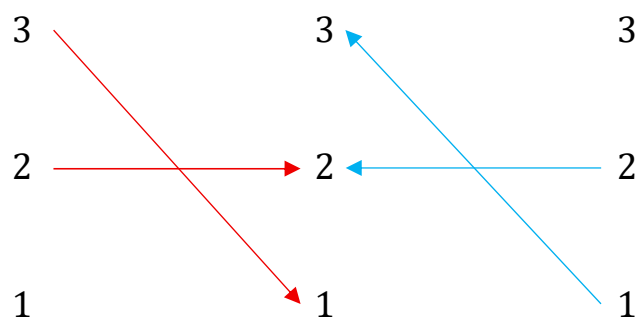
$$4. DS = [(3.1, 2.2, 1.1) \times (1.1, 2.2, 1.3)]$$



$$5. DS = [(3.1, 2.2, 1.2) \times (2.1, 2.2, 1.3)]$$

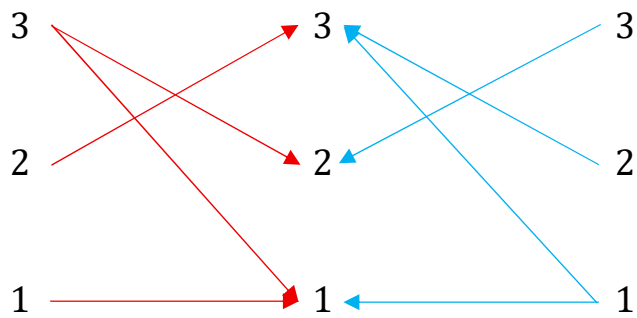


$$6. DS = [(3.1, 2.2, 1.3) \times (3.1, 2.2, 1.3)]$$

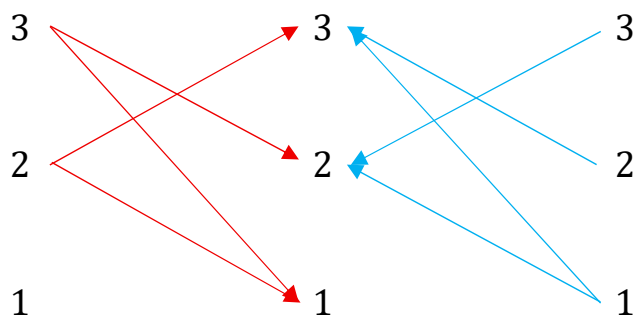


2.3. Dritte TT

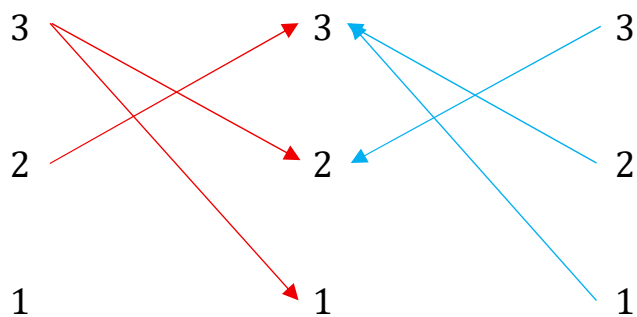
$$7. DS = [(3.1, 2.3, 1.1) \times (1.1, 3.2, 1.3)]$$



$$8. DS = [(3.1, 2.3, 1.2) \times (2.1, 3.2, 1.3)]$$

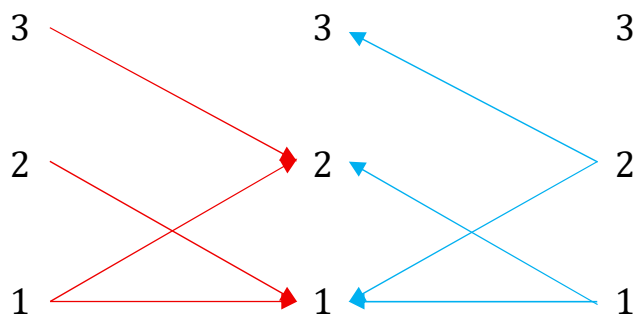


$$9. DS = [(3.1, 2.3, 1.3) \times (3.1, 3.2, 1.3)]$$

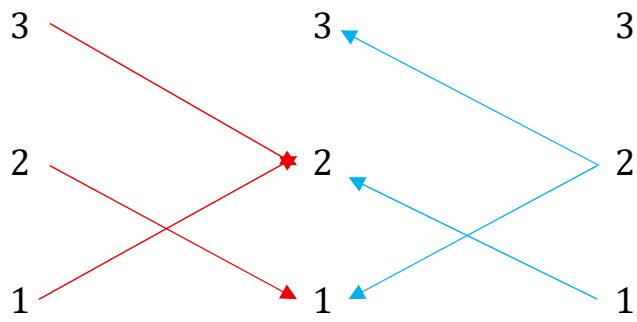


2.4. Vierte TT

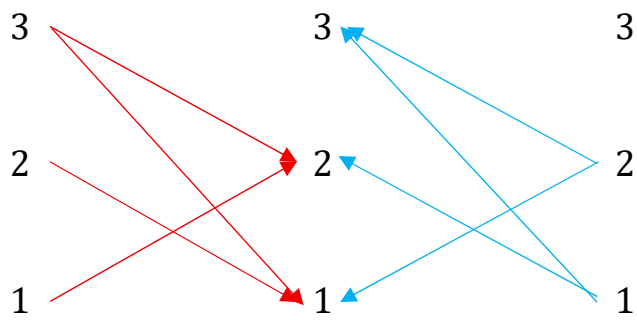
$$10. DS = [(3.2, 2.1, 1.1) \times (1.1, 1.2, 2.3)]$$



$$11. DS = [(3.2, 2.1, 1.2) \times (2.1, 1.2, 2.3)]$$

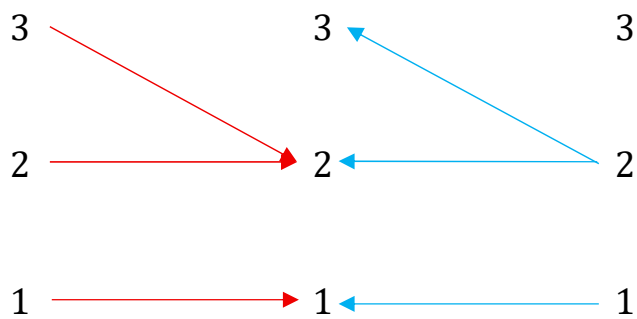


$$12. DS = [(3.2, 2.1, 1.3) \times (3.1, 1.2, 2.3)]$$

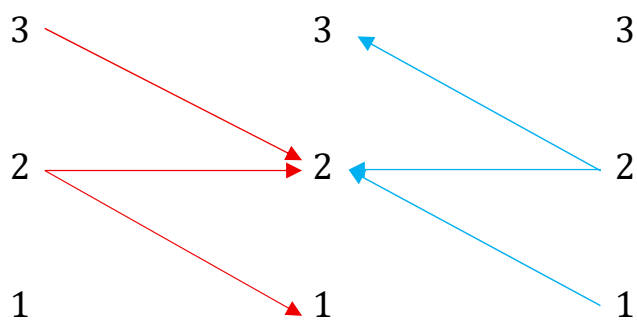


2.5. Fünfte TT

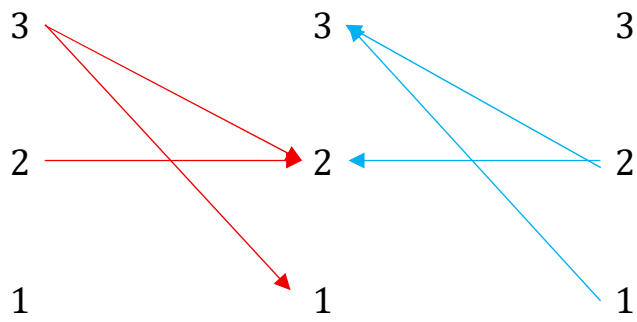
$$13. DS = [(3.2, 2.2, 1.1) \times (1.1, 2.2, 2.3)]$$



$$14. DS = [(3.2, 2.2, 1.2) \times (2.1, 2.2, 2.3)]$$

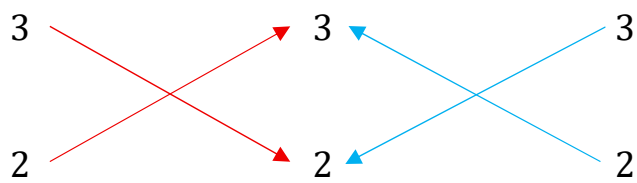


$$15. DS = [(3.2, 2.2, 1.3) \times (3.1, 2.2, 2.3)]$$

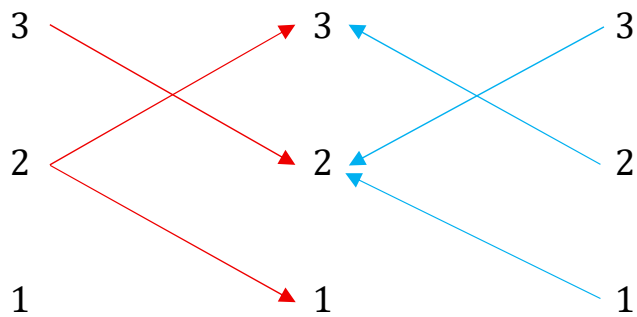


2.6. Sechste TT

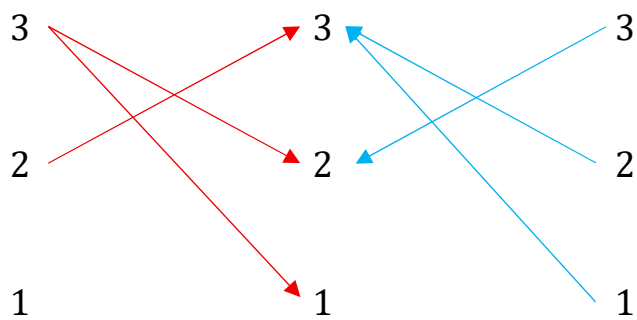
$$16. DS = [(3.2, 2.3, 1.1) \times (1.1, 3.2, 2.3)]$$



$$17. DS = [(3.2, 2.3, 1.2) \times (2.1, 3.2, 2.3)]$$

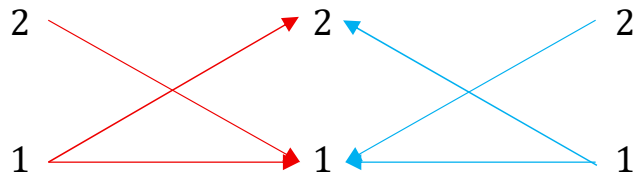


$$18. DS = [(3.2, 2.3, 1.3) \times (3.1, 3.2, 2.3)]$$

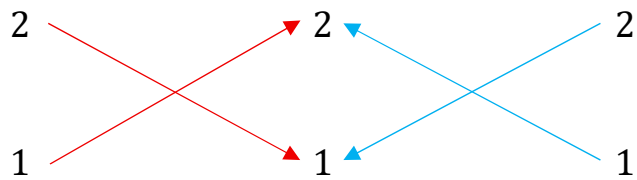


2.7. Siebente TT

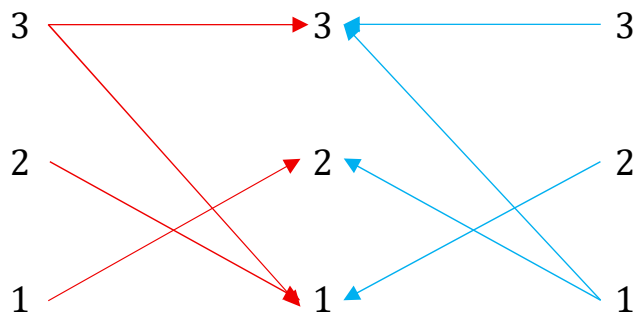
$$19. DS = [(3.3, 2.1, 1.1) \times (1.1, 1.2, 3.3)]$$



$$20. DS = [(3.3, 2.1, 1.2) \times (2.1, 1.2, 3.3)]$$



$$21. DS = [(3.3, 2.1, 1.3) \times (3.1, 1.2, 3.3)]$$

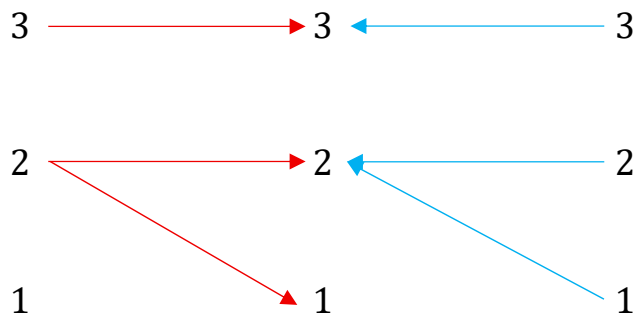


2.8. Achte TT

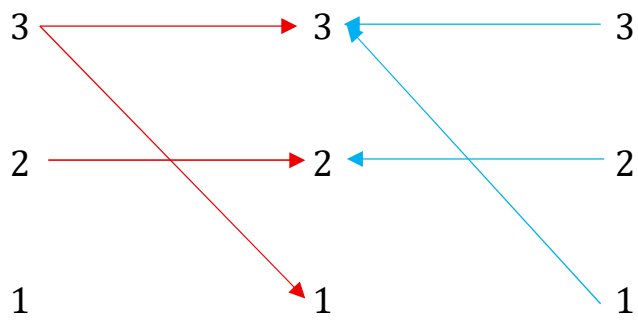
$$22. DS = [(3.3, 2.2, 1.1) \times (1.1, 2.2, 3.3)]$$



$$23. DS = [(3.3, 2.2, 1.2) \times (2.1, 2.2, 3.3)]$$

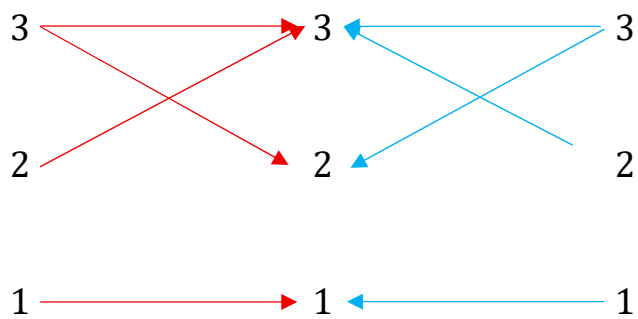


$$24. DS = [(3.3, 2.2, 1.3) \times (3.1, 2.2, 3.3)]$$

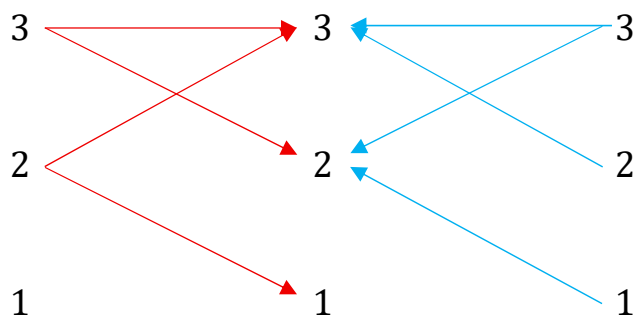


2.9. Neunte TT

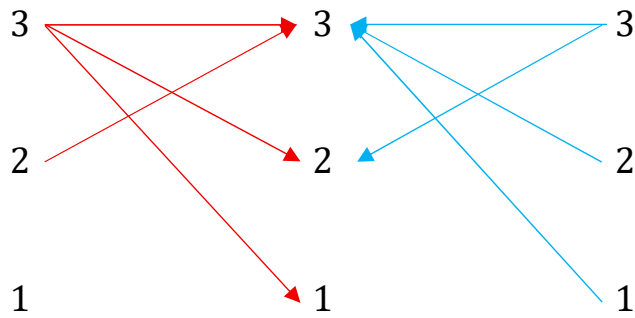
$$25. DS = [(3.3, 2.3, 1.1) \times (1.1, 3.2, 3.3)]$$



$$26. DS = [(3.3, 2.3, 1.2) \times (2.1, 3.2, 3.3)]$$



$$27. DS = [(3.3, 2.3, 1.3) \times (3.1, 3.2, 3.3)]$$



Literatur

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22.8.2025